Solution of a generalized Riemann boundary value problem with a Carleman shift in the real line

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Abstract

In the real line we consider singular integral operators with a linear Carleman shift and complex conjugation, acting in $\tilde{L}_2(\mathbb{R})$, the space of all Lebesgue measurable complex value functions on \mathbb{R} with p = 2 power. We show that the original singular integral operator with shift and conjugation is, after extension, equivalent to a singular integral operator without shift and with a 4×4 square matrix coefficients. By exploiting the properties of the factorization of the symbol of this last operator, it is possible to describe the solution of a generalized Riemann boundary value problem with a Carleman shift.