# PUBLIC VERIFIABLE SECRET SHARING AND APPLICATIONS TO RANDOMNESS BEACONS

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ABSTRACT. In this talk I will review some recent advances on the topic of publicly verifiable secret sharing and its applications to the construction of randomness beacons. The talk is based on a series of works in collaboration with Bernardo David, Lydia Garms, Anders Konring, Omer Shlomovits and Denis Varlakov.

## SUMMARY

Secret sharing schemes allow a dealer to distribute the knowledge of a secret among a number of parties according to certain access conditions (for example, that only a large enough subset of the parties can reconstruct the secret when they agree in doing so). Secret sharing schemes constitute one of the most well known cryptographic primitives.

In publicly verifiable secret sharing (PVSS), introduced in [1], the dealer publishes the shares in an encrypted form, and proves that these ciphertexts indeed hide a set of valid shares (i.e. a secret can be reconstructed from these shares) in such a way that any external verifier can be convinced of the validity of the sharing without obtaining information about the secret. In this way a PVSS scheme is a cryptographic commitment to a secret, that can be jointly opened by a large enough number of share receivers. PVSS has applications in electronic voting, multiparty computation and recently in the construction of distributed randomness beacons for its use in proof-of-stake blockchains. One notable work was [2] who introduced a simple construction for PVSS based on discrete logarithm hardness assumptions.

This talk will review a line of work ([3, 4, 5, 6]) starting in 2017 where we have subsequently reduced the complexity of PVSS and thereby improved its scalability for large number of parties, which is motivated especially by the aforementioned applications to distributed randomness beacons and other related uses. I will detail some of these efficiency improvements and briefly discuss how to utilize this tool to construct distributed randomness beacons.

### References

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## IGNACIO CASCUDO

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